

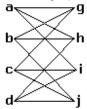
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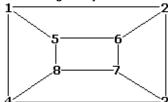
# **FORBIDDEN SUBGRAPH**

Two undirected graphs G and H are said to be isomorphic if:

- they have the same number of vertices and
- a one-to-one correspondence exists between their vertices so that, for any two distinct vertices of *G*, there exists an edge between them if and only if there exists an edge between their corresponding vertices in *H*.

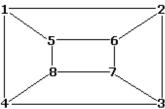
For example, the next two graphs are isomorphic, even though they look different here:

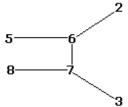




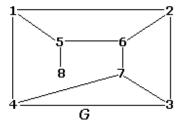
A possible one-to-one correspondence showing that these two graphs are isomorphic is given by {a-1, b-6, c-8, d-3, g-5, h-2, i-4, j-7}, but others exist too.

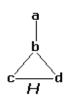
A *subgraph* of a graph *G* is a graph whose sets of vertices and edges are subsets of those in *G*. Note that *G* is a subgraph of itself. The following example shows a graph and one of its subgraphs:

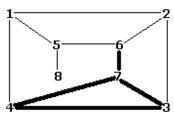




We say that a graph G contains another graph H if there is at least one subgraph H of G which is isomorphic to H. The following figure shows a graph G that contains the graph H.







# **TASK**

Given two undirected graphs *G* and *H*, produce a subgraph *G* of *G* such that:

- the number of vertices in G and G' is the same and
- H is **not** contained in G'.

Naturally, there may be many subgraphs G' with the above properties. Produce one of those subgraphs with as many edges as possible.



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## **BASE ALGORITHM**

Perhaps the most basic strategy to approach this problem is to consider the edges of G in the order that they are represented in the input file, then attempting to add them one by one to G, verifying at each step whether H is contained in G or not. The correct implementation of this greedy algorithm will earn some points, but much better strategies exist.

#### **CONSTRAINTS**

 $3 \le m \le 4$  The number of vertices of *H*.  $3 \le n \le 1000$  The number of vertices of *G*.

### **INPUT**

You will be given 10 files forbidden1.in to forbidden10.in each with the following data:

forbiddenK.in	DESCRIPTION
3 5	<b>LINE 1:</b> Contains two space-separated integers, respectively: <i>m</i> and
0 1 0	n.
1 0 1	<b>NEXT m LINES:</b> Each line contains <i>m</i> space-separated integers and
0 1 0	represents one vertex of H in the order 1,, m. The i-th element
0 1 0 0 0	of the <i>j</i> -th line in this section is equal to 1 if vertices <i>i</i> and <i>j</i> are
1 0 1 0 0	joined by an edge in <i>H</i> and is equal to 0 otherwise.
0 1 0 1 0	<b>NEXT n LINES:</b> Each line contains <i>n</i> space-separated integers and
0 0 1 0 1	represents one vertex of <i>G</i> in the order 1,, <i>n</i> . The <i>i</i> -th element
0 0 0 1 0	of the <i>j</i> -th line in this section is equal to 1 if vertices <i>i</i> and <i>j</i> are
	joined by an edge in G and is equal to 0 otherwise.

Observe that, except for line 1, the above input represents the adjacency matrices of H and G.

## OUTPUT

You must provide 10 files, one for each of the inputs. Each file must contain the following data:

forbiddenK.out	DESCRIPTION
#FILE forbidden K	LINE 1: The file header. The file header must contain
5	#FILE forbidden K
0 1 0 0 0	where K is a number between 1 and 10 that corresponds to the
1 0 0 0 0	input file solved.
0 0 0 0 0	LINE 2: Contains one integer: n.
0 0 0 0 0	<b>NEXT n LINES:</b> Each line contains <i>n</i> space-separated integers and
0 0 0 0 0	represents one vertex of <i>G</i> ' in the order 1,, <i>n</i> . The <i>i</i> -th element
	of the <i>j</i> -th line in this section is equal to 1 if vertices <i>i</i> and <i>j</i> are
	joined by an edge in G', and is 0 otherwise.

Observe that, except for lines 1 and 2, the above output represents the adjacency matrix of G'. Note that there are many possible outputs, and that the above output is correct but not optimal.

### **GRADING**

Your score will depend on the number of edges in the G'you output. Your score will be determined in the following way: you will receive a non-zero score for each output file only if it meets the task specification. If it does, your score will be calculated as follows. Let  $E_y$  be the number of edges in your output, let  $E_b$  be the number of edges in G' as computed by the BASE ALGORITHM, and let  $E_m$  be the maximum number of edges in the output of any of the contestants submissions. Your score for the case will be:

- $30 E_v / E_b$  if  $E_v \le E_b$ , or
- $30 + 70(E_v E_b)/(E_m E_b)$  if  $E_v > E_b$ .