English
Version 1.2

## FORBIDDEN SUBGRAPH

Two undirected graphs $G$ and $H$ are said to be isomorphic if:

- they have the same number of vertices and
- a one-to-one correspondence exists between their vertices so that, for any two distinct vertices of $G$, there exists an edge between them if and only if there exists an edge between their corresponding vertices in $H$.

For example, the next two graphs are isomorphic, even though they look different here:


A possible one-to-one correspondence showing that these two graphs are isomorphic is given by \{a-1, b-6, c-8, d-3, g-5, h-2, i-4, j-7\}, but others exist too.

A subgraph of a graph $G$ is a graph whose sets of vertices and edges are subsets of those in $G$. Note that $G$ is a subgraph of itself. The following example shows a graph and one of its subgraphs:


We say that a graph $G$ contains another graph $H$ if there is at least one subgraph $H^{\prime}$ of $G$ which is isomorphic to $H$. The following figure shows a graph $G$ that contains the graph $H$.




## TASK

Given two undirected graphs $G$ and $H$, produce a subgraph $G$ ' of $G$ such that:

- the number of vertices in $G$ and $G^{\prime}$ is the same and
- $\quad H$ is not contained in $G^{\prime}$.

Naturally, there may be many subgraphs G' with the above properties. Produce one of those subgraphs with as many edges as possible.

## BASE ALGORITHM

Perhaps the most basic strategy to approach this problem is to consider the edges of $G$ in the order that they are represented in the input file, then attempting to add them one by one to $G^{\prime}$, verifying at each step whether $H$ is contained in $G^{\prime}$ or not. The correct implementation of this greedy algorithm will earn some points, but much better strategies exist.

## CONSTRAINTS

$3 \leq m \leq 4 \quad$ The number of vertices of $H$.
$3 \leq n \leq 1000$ The number of vertices of $G$.
INPUT
You will be given 10 files forbidden1. in to forbidden10. in each with the following data:


Observe that, except for line 1, the above input represents the adjacency matrices of $H$ and $G$.
OUTPUT
You must provide 10 files, one for each of the inputs. Each file must contain the following data:

| forbiddenK.out | DESCRIPTION |
| :---: | :---: |
| ```#FILE forbidden K 5 0 1 0 0 0``` | LINE 1: The file header. The file header must contain \#FILE forbidden K where K is a number between 1 and 10 that corresponds to the |
| $\begin{array}{llll}1 & 1 & 0 & 0 \\ 0 & 0 & 0\end{array}$ | where $K$ is a number between 1 and 10 that corresponds to the input file solved. |
| 00000 | LINE 2: Contains one integer: $n$. |
| $\begin{array}{lllll} 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \end{array}$ | NEXT n LINES: Each line contains $n$ space-separated integers and represents one vertex of $G^{\prime}$ in the order $1, \ldots, n$. The $i$-th element of the $j$-th line in this section is equal to 1 if vertices $i$ and $j$ are joined by an edge in $G^{\prime}$, and is 0 otherwise. |

Observe that, except for lines 1 and 2, the above output represents the adjacency matrix of $G^{\prime}$. Note that there are many possible outputs, and that the above output is correct but not optimal.

## GRADING

Your score will depend on the number of edges in the G' you output. Your score will be determined in the following way: you will receive a non-zero score for each output file only if it meets the task specification. If it does, your score will be calculated as follows. Let $E_{y}$ be the number of edges in your output, let $E_{b}$ be the number of edges in $G^{\prime}$ as computed by the BASE ALGORITHM, and let $E_{m}$ be the maximum number of edges in the output of any of the contestants submissions. Your score for the case will be:

- $30 E_{y} / E_{b}$ if $E_{y} \leq E_{b}$, or
- $30+70\left(E_{y}-E_{b}\right) /\left(E_{m}-E_{b}\right)$ if $E_{y}>E_{b}$.

